

Augmentation of Vortex Lift by Spanwise Blowing

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An investigation has been conducted to evaluate the aerodynamic effects associated with blowing a jet spanwise over a wing's upper surface in a direction parallel to the leading edge. Experimental pressure and force data were obtained on wings with sweep angles of 30° and 45° , and showed that spanwise blowing aids in the formation and control of the leading-edge vortex, and, hence, significantly improves the aerodynamic characteristics at high angles of attack. Full vortex section lift is achieved at the inboard span station with a small blowing rate, but successively higher blowing rates are necessary to attain the full vortex-lift level at increased span distances. Spanwise blowing generates large increases in lift at high angles of attack, improves the drag polars, and extends the linear pitching moment to high lifts. These aerodynamic characteristics are estimated with the leading-edge suction analogy. Integration of the spanwise blowing concept into a fighter aircraft design offers the possibility of increasing specific excess power available for maneuvering at higher load factors.

Nomenclature

A	= aspect ratio
a/l	= notch ratio (see Fig. 8)
b	= span
c_d, c_l	= section drag and lift coefficients
c_r	= chord at wing-fuselage juncture
$c_{l,p}, c_{l,v}$	= potential and vortex section lift coefficients
$c_{l,tot}$	= $c_{l,p} + c_{l,v}$
$C_{D,L}$	= aerodynamic drag-due-to-lift coefficient
C_L	= aerodynamic lift coefficient
C_m	= aerodynamic pitching-moment coefficient
$C_{L,0}$	= aerodynamic lift coefficient without blowing
$C_{L,p}$	= potential lift coefficient
$C_{L,tot}$	= sum of potential and vortex lift coefficients
C_μ	= nozzle momentum coefficient, $wV_j/gq_\infty S$
C_T	= nozzle thrust coefficient, static thrust/ $q_\infty S$
ΔC_p	= difference between upper and lower surface pressure coefficients
ΔC_L	= jet-on lift minus jet-off lift
d	= nozzle diameter
g	= gravity
h	= height of nozzle center line above wing surface
LE	= leading edge
M_∞	= freestream Mach number
q_∞	= freestream dynamic pressure
S	= wing reference area
V_j	= jet velocity due to isentropic expansion to freestream static pressure
V_∞	= freestream velocity
w	= nozzle-air weight flow
x_n	= chordwise distance of nozzle from LE of wing root chord (c_r)
y	= spanwise distance, measured from model plane of symmetry
α	= angle of attack
Λ_{LE}	= sweep angle of wing leading edge

Introduction

ON thin, highly sweptback wings at moderate-to-high angles of attack, the flow is characterized by a leading-edge separation which forms a stable vortex over the wing and

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provides large vortex-lift increments. This characteristic of slender wings, of the supersonic cruise type, has been understood for many years. However, for moderately swept wings that have higher aspect ratios and are suitable for fighter aircraft, vortex breakdown occurs at low α 's. Thus, the wing does not achieve the large vortex-lift increments that are desirable for subsonic maneuvering. These trends are illustrated in Fig. 1, which shows the effect of leading-edge sweep on the lift of flat-plate delta wings at $\alpha = 20^\circ$.

A promising technique for enhancing the leading-edge vortex and effectively delaying vortex breakdown to higher angles of attack is that of spanwise blowing. This concept consists of blowing a discrete jet spanwise over the wing's upper surface in a direction essentially parallel to the leading edge. The interaction of this jet flow with the separated flow from the wing leading edge results in the formation and control of the leading-edge vortex, with a subsequent increase in lift. Some original research related to this concept was performed by Werle¹ and Cornish² who demonstrated the control of separated flow regions by transverse blowing. The additional work reported by Dixon et al.,³⁻⁵ and Bradley et al.,⁶ applied the concept to different types of lifting surfaces, such as wings, leading- and trailing-edge flaps, and rudders.

In order to supplement this previous research, two wind-tunnel test programs were conducted to determine the effects of spanwise blowing on wings of interest for fighter aircraft applications, that is, where the wings have moderate sweep angles and moderate-to-high aspect ratios. The first wind-tunnel investigation obtained wing-surface pressure distributions on a trapezoidal wing with a leading-edge sweep

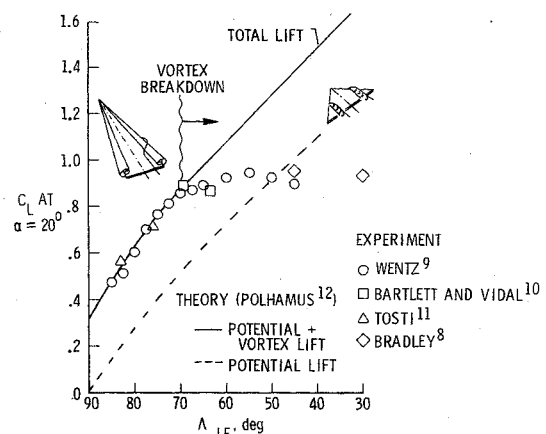


Fig. 1 Lift capability of delta wings at $\alpha = 20^\circ$.

angle (Λ_{LE}) of 44° . Lift, drag, and pitching moment were measured in the second test program on delta, arrow, and diamond wing planforms having Λ_{LE} of 30° and 45° . These tests were performed at a freestream Mach number of about 0.2 with spanwise blowing from the fuselage only (no ducting in the wings). Data were acquired for a range of angle of attack and jet thrust coefficient.

While specific information about these pressure and force tests is contained in Refs. 7 and 8, respectively, the current paper will summarize some of the research highlights that illustrate the effects of spanwise blowing on the wing's surface pressure distribution, spanwise development of vortex section lift, longitudinal aerodynamic characteristics, angle of attack for vortex breakdown, and specific excess power available for maneuvering.

Results and Discussion

The objective of blowing spanwise on moderately swept wings is to artificially induce spanwise flow gradients similar to those that appear naturally on highly swept wings,⁹⁻¹² such as the delta wing sketched in Fig. 1. The flow gradients resulting from blowing are favorable for the formation and control of the leading-edge vortex, as has been demonstrated in Ref. 13. In the following sections, an effort is made to examine the effects of this complicated jet-vortex flow system on wing pressures and forces.

Pressure Tests

The wing-body model utilized for the pressure tests is illustrated in Fig. 2. It had a trapezoidal wing with a leading-edge sweep of 44° , an aspect ratio of 2.5, and a taper ratio of 0.2. In addition, the wing had no twist, camber, or dihedral, and had a circular arc airfoil section (measured streamwise) with sharp leading and trailing edges. The wing thickness ratio was 6% at the fuselage-wing junction and varied linearly to 4% at the wing tip. The upper and lower surfaces of the wing were instrumented with 140 pressure orifices arranged in chordwise rows at six different span locations.

The tests were conducted in the Langley high-speed 7 by 10 ft wind tunnel at a Mach number of 0.26 and a Reynolds number of 5.2×10^6 per meter. Data were obtained for a range of model angle of attack and jet blowing rate for the model without fixed transition. Although a variety of nozzle orientations were examined in Ref. 7, the present paper discusses only those data that were obtained with $h/d=0.835$, $x_n/c_r=0.23$, and $\Lambda_n=44^\circ$.

The primary nozzle parameter that is used herein to identify various jet blowing rates is the jet thrust coefficient, C_T . This coefficient uses the static nozzle thrust which was obtained as a function of plenum pressure by calibrating the nozzles. Additional details concerning the tests can be obtained from Ref. 7.

Wing-Pressure Field

Detailed pressure distributions are presented in Ref. 7 and show that spanwise blowing results in significant effects on

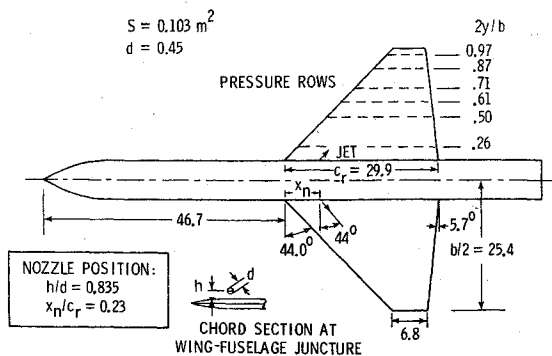


Fig. 2 Model geometry for pressure tests (all dimensions are in centimeters).

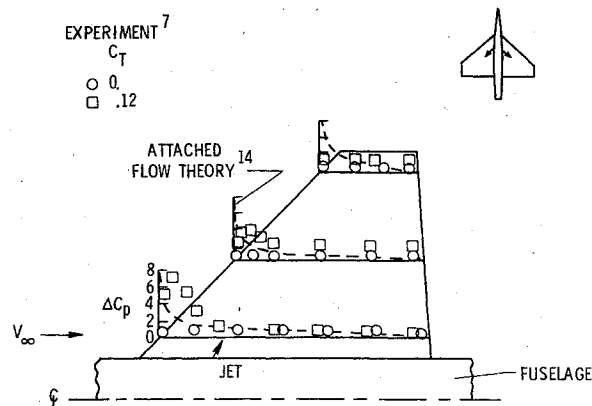


Fig. 3 Schematic of wing pressure field for $\alpha = 24^\circ$.

the wing upper-surface pressure field with little effect on the lower-surface pressures, and at high α 's as opposed to low α 's. A schematic of the wing pressure field is presented in Fig. 3 for $\alpha = 24^\circ$ and illustrates some of the primary features of the spanwise blowing process.

The attached flow theory is presented in Fig. 3 to show what the pressure distribution might be if the flow remained attached at the leading edge. This attached flow condition is represented by the subsonic theory from Ref. 14, and is characterized by negatively increasing ΔC_p as the leading edge is approached. The experimental data obtained with no blowing ($C_T=0$) show that the flow cannot negotiate the sharp leading edge and, therefore, separates. In fact for this α , the ΔC_p values are essentially constant, which is indicative of separated flow over the entire upper surface.

Spanwise blowing ($C_T=0.12$) results in significant decreases in ΔC_p at the inboard span station and near the wing leading edge. These high suction pressures are a result of the formation of a strong leading-edge vortex, where the flow reattaches to the wing surface at some point aft of the jet flow. At larger $2y/b$, the jet-vortex system weakens, which results in decreases in the peak pressure near the leading edge and a spreading of the influence over all the wing section. Reference 7 showed that larger C_T values increased $-\Delta C_p$ as well as the spanwise extent of the jet's effect. This suggests that the jet will have the most beneficial effect at that point where the jet and vortex are close to their respective origins, that is, where the jet flow is strong enough to result in vortex rollup and the vortex is still close to the wing surface. These pressure results are similar to those obtained on a rectangular flat plate in Ref. 3. The pressure distributions obtained with blowing appear to be similar to those obtained on highly-swept delta wings which have a natural (no blowing required) leading-edge vortex.

Section Force

The chordwise pressure distributions were numerically fitted with a cubic spline and then integrated to obtain the section forces (Ref. 7 also includes section pitching moments). The effects of spanwise blowing on section lift curves are presented in Fig. 4 for the wing span station $2y/b=0.5$. These data show that spanwise blowing increases c_l throughout the α range, the largest effect occurring for the largest C_T and at high α , where section stall has occurred with no blowing ($C_T=0$). The nonlinearity in c_l vs α that results when there is blowing is typical of sections developing vortex lift.

To better interpret these experimental results, theoretical estimates of the section lift characteristics were made by using the leading-edge suction analogy developed by Polhamus.¹⁵ The basic assumptions which are used in Ref 15 to apply the suction analogy to a wing with a fully developed leading-edge vortex are assumed to apply here on a sectional basis. Ac-

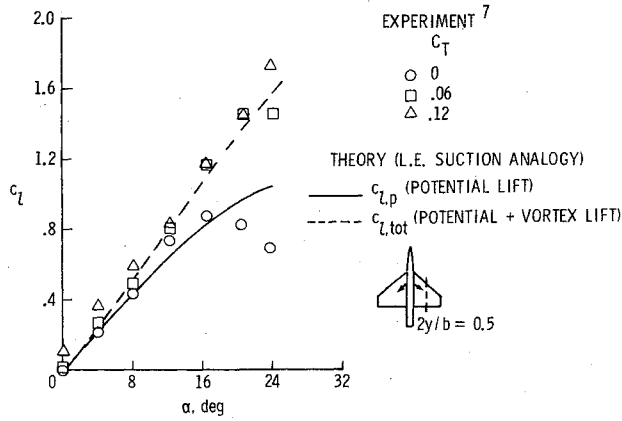


Fig. 4 Effect of spanwise blowing on section lift curves at $2y/b = 0.5$.

cordingly, for a section with no leading-edge suction, the potential and vortex section lifts are given by:

$$c_{l,p} = k_p \sin \alpha \cos^2 \alpha \quad (1)$$

$$c_{l,v} = k_v \sin^2 \alpha \cos \alpha \quad (2)$$

where the total lift is

$$c_{l,tot} = c_{l,p} + c_{l,v} \quad (3)$$

The terms k_p and k_v are defined as

$$k_p = c_{l,\alpha} \quad (4)$$

and

$$k_v = \frac{c_l}{\cos \Lambda_{LE} \sin^2 \alpha} = \frac{c_s}{\sin^2 \alpha} \quad (5)$$

where c_l and c_s are the section thrust and suction-force coefficients, respectively. Because of their dependence on section properties, the parameters k_p and k_v are functions of spanwise location. The parameters c_l , c_s , and $c_{l,\alpha}$ were determined at different span stations on the trapezoidal wing by the lifting surface theory of Ref. 16. Since Ref. 16 is a linear theory, k_v was calculated by using α^2 in Eq. (5) instead of $\sin^2 \alpha$.

The theoretical estimates for section lift with no vortex lift ($c_{l,p}$) and with full vortex lift ($c_{l,tot}$) are shown in Fig. 4. With no blowing, the section has little or no leading-edge vortex flow. The dashed line represents the estimated section lift that would result if the leading-edge vortex was fully established, and has essentially the same lift-curve slopes as the data with blowing. The lift values are estimated reasonably well if the jet-induced camber effect, noted at $\alpha = 0^\circ$, is accounted for. This induced camber effect is dependent on C_T as well as the $2y/b$ station (see Ref. 7), and has been observed in other investigations.^{3,5}

So far, the data have shown that the amount of sectional vortex lift generated by spanwise blowing is dependent on C_T , $2y/b$, and α . One question that should be considered is what value of C_T does it take to achieve the full vortex-lift level at a given span station. This is demonstrated in Fig. 5 where c_l is plotted as a function of C_T for the span station at $2y/b = 0.5$ and $\alpha = 24^\circ$. Increasing the jet blowing rate increases c_l from the basic wing lift value up to and beyond the full vortex-lift level estimated by the suction analogy. For this particular span station, a C_T of about 0.08 is required to achieve the full vortex lift. The data of Ref. 7 indicate, as one might expect, that progressively higher values of C_T are required to obtain this lift level at larger span distances. The trends discussed for Fig. 5 are also demonstrated in Fig. 6, which presents the spanwise variation of section lift for a range of C_T values with the model at $\alpha = 24^\circ$. Increases in the

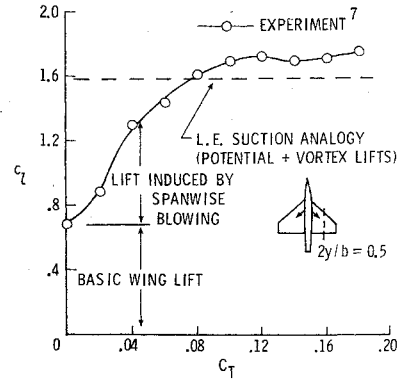


Fig. 5 Variation of section lift with C_T for $\alpha = 24^\circ$ and $2y/b = 0.5$.

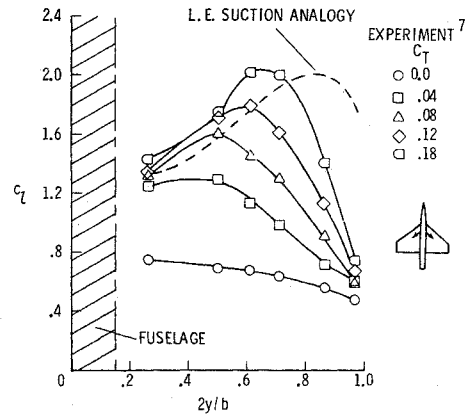


Fig. 6 Effect of C_T on spanwise variation of section lift for $\alpha = 24^\circ$.

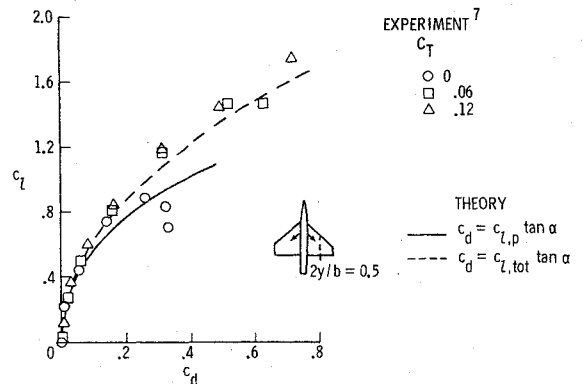


Fig. 7 Effect of spanwise blowing on section induced-drag characteristics at $2y/b = 0.5$.

blowing rate results in progressive changes in the shape of the c_l distribution from the distribution with no blowing, which in this case is typical of a wing with separated upper-surface flow, to the c_l distribution estimated by the suction analogy. At the higher blowing rates, the section lift values on the inboard portion of the wing are higher than the theoretical estimates. This jet-induced effect, coupled with available vortex lift on the outboard portion of the wing, suggests that higher blowing rates than those used in this test will produce even higher lift levels.

The results of Figs. 3-6 suggest that blowing spanwise from the fuselage is a jet-decay problem,⁵ which implies that the development of the leading-edge vortex and the associated vortex section lift are strongly dependent on the local jet and vortex flow properties, as well as the freestream velocity. As a matter of reference, the wing and jet geometries of the current study are such that the jet flow must penetrate almost 62 nozzle-exit diameters to reach the wing tip. The resulting decay of

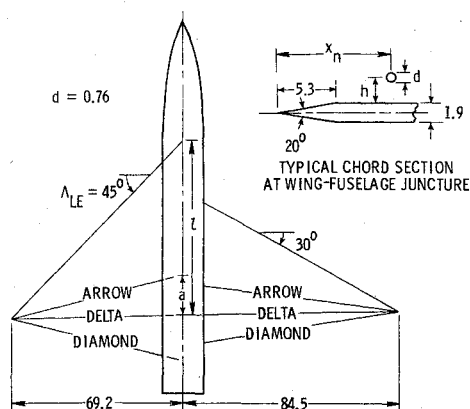


Fig. 8 Model geometry for force tests (all dimensions are in centimeters).

the jet velocity is large enough to have a significant effect on the formation of the leading-edge vortex.

The effect of spanwise blowing on the section induced-drag characteristics is presented in Fig. 7 for $2y/b=0.5$. It is observed that blowing improves the drag polars, particularly at high c_l . Estimates for these polars were obtained by taking the section normal force to be the resultant section force, which should be appropriate for the zero LE suction assumption. The theory provides reasonable predictions of induced-drag for the configuration with and without blowing. At high c_l , the measured c_d is lower than the predicted level, which is consistent with the lift results discussed in Fig. 4.

Force Tests

The wind-tunnel model utilized for the force tests is illustrated in Fig. 8, and consisted of a body-of-revolution fuselage with delta, arrow, and diamond wing planforms having Λ_{LE} of 30° and 45° . The wings were flat plates having sharp leading edges and no tip chord. The aspect ratio, reference wing area, and notch ratio are listed in Table 1 for all of the wing configurations. The origin of the stability axis system is defined at 25% of the mean aerodynamic chord for each wing.

The tests were conducted in the General Dynamics Low-Speed Wind Tunnel at a Mach number of 0.2 and a Reynolds number of 4.6×10^6 per meter. The sweep angle for the spanwise blowing nozzles corresponded to the wing leading-edge sweep angle. Various chordwise and vertical nozzle positions were investigated in Ref. 8 and resulted in the position, $x_n/c_r = 0.4$ and $h/d = 1.5$ used for the family of wings. The jet momentum coefficient C_μ is used herein to correlate the effects of blowing. Further details of these tests can be obtained from Ref. 8.

Aerodynamic Characteristics

The effects of spanwise blowing on the aerodynamic lift characteristics of the 45° swept delta, arrow, and diamond-wing configurations are illustrated in Fig. 9, and are representative of the 30° swept family of planforms. These data show only the aerodynamic effects of spanwise blowing, since the thrusting effects have been subtracted out. The reader is

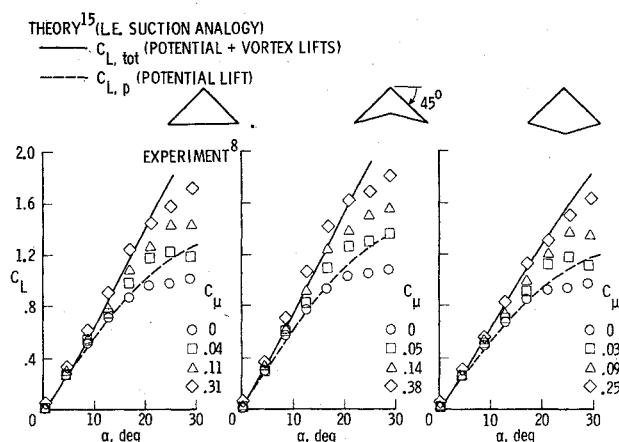


Fig. 9 Effect of spanwise blowing on aerodynamic lift characteristics of 45° swept delta, arrow, and diamond wings.

referred to Ref. 8 for the total forces and moments obtained on all of the wing planforms.

The data in Fig. 9 were obtained for a range of C_μ values and show that spanwise blowing has a very favorable effect on the lift characteristics, the primary benefits occurring at moderate-to-high angles of attack. Increasing the blowing rate increases the maximum C_L , as well as the angle of attack where this maximum lift is achieved. These high- α lift trends would be expected from the pressure results discussed in the first part of this paper.

The leading-edge suction analogy was used to estimate lift assuming the wing does (solid line) or does not (dashed line) develop vortex lift. Comparing these theoretical lift results with the experimental data shows that with no blowing, the wings develop a small amount of vortex lift at low angles of attack, but no vortex lift at higher α 's. Blowing tends to enhance the development of the leading-edge vortex so that vortex breakdown is delayed and vortex lift is generated. Increasing the blowing rate results in increases in the vortex-lift contribution until the full vortex-lift level is achieved.

At the higher blowing rates, the measured lifts are higher than the estimated values, which is due to jet-induced effects. At low angles of attack, several studies^{3,7,8} have associated this interference lift with an "effective" camber increase. Investigation of the current data showed that the C_L at $\alpha = 0^\circ$ increased with increases in C_μ for all of the wing planforms, and that this increment of lift was not necessarily constant throughout the angle-of-attack range. If the C_L value at $\alpha = 0^\circ$ is added to the vortex-lift theoretical values, the adjusted theory yields good predictions for the experimental lifts and therefore, provides a theoretical upper bound for the lifts that can be expected due to spanwise blowing for the range of C_μ values investigated here.

The effects of spanwise blowing on drag-due-to-lift and pitching moment for the 45° delta wing are presented in Fig. 10 and typify the results obtained with the other wing planforms. As can be seen, blowing improves the drag polars and extends the linear pitching moment to higher C_L 's. The experimental data compare favorably with the drag polar and pitching-moment curve estimated by the leading-edge suction

Table 1 Wing geometry for force tests

Planform	$\Lambda_{LE} = 30^\circ$			$\Lambda_{LE} = 45^\circ$		
	A	S, m^2	a/l	A	S, m^2	a/l
Delta	6.93	0.412	0.00	4.00	0.479	0.00
Arrow	9.24	0.309	0.25	5.33	0.359	0.25
Diamond	5.54	0.515	-0.25	3.20	0.599	-0.25

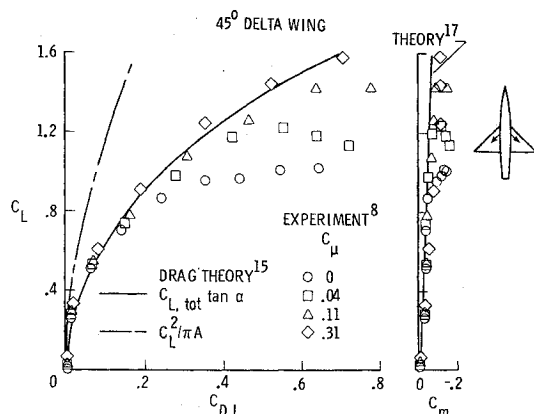


Fig. 10 Effect of blowing on drag and pitching moment of the 45° delta wing.

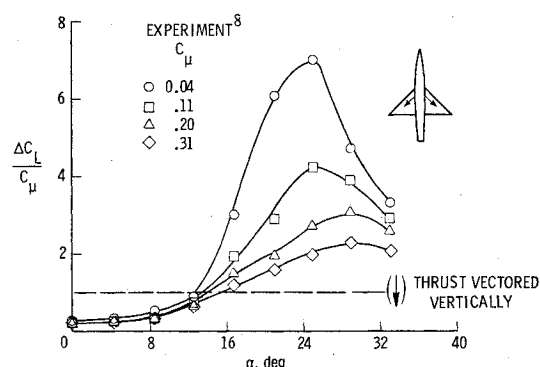


Fig. 11 Effect of α and C_μ on lift augmentation ratio for the 45° delta wing.

analogy.^{15,17} It is observed that at low-to-moderate lifts, the drag-due-to-lift data are lower than the zero-suction vortex-lift polar, and, in fact, approach the full-suction polar given by $C_L^2/\pi A$. The wing apparently develops a sizable leading-edge suction force without blowing. This may seem unreasonable since the wing has a beveled sharp leading edge, but the flat-plate model is apparently thick enough to allow some amount of thrust recovery. The drag-due-to-lift effects noted here for the 45° swept wing are appropriately larger for 30° swept planforms.⁸ Bradley⁶ has indicated that these results may be duplicated with small LE flap deflections and used in conjunction with vortex-lift augmentation to improve the drag polar.

Lift Effectiveness

One way to judge the lifting efficiency of spanwise blowing is by examining the lift augmentation ratio, $\Delta C_L/C_\mu$. The effect of α and C_μ on this parameter is presented in Fig 11. Increasing α increases the augmentation ratio from the minimum value at $\alpha=0^\circ$ (this value would be zero if there were no jet-induced camber effect) to a maximum value at angles of attack from 25° to 30° (depending on C_μ). The largest augmentation ratio of 7 was obtained with the lowest C_μ value, which means that spanwise blowing generates seven times the lift that would be obtained if the jet were vectored downward (perpendicular to the freestream). Increasing the blowing rate decreases the lifting efficiency of spanwise blowing, a trend that is typical of most jet augmentation systems. These data suggest that spanwise blowing becomes more effective in producing lift than thrust vectoring at angles of attack above 13° to 16° (depending on C_μ). These results are typical of the other planform configurations, although the magnitudes may change somewhat.

The effect of sweep angle on the jet-induced lift is shown in Fig. 12 for delta wings at $\alpha=21^\circ$, where the parameter

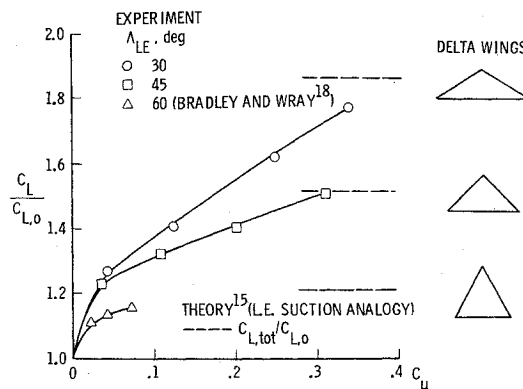


Fig. 12 Effect of Λ_{LE} on the lift effectiveness of blowing on delta wing planforms at $\alpha=21^\circ$.

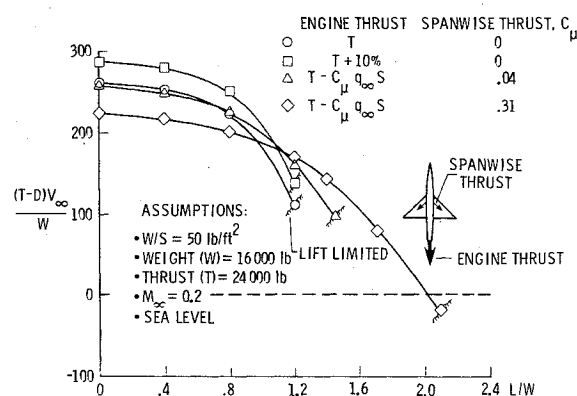


Fig. 13 Effect of spanwise blowing on specific excess power available for maneuvering the 45° delta-wing configuration. Note: Lift (L) and drag (D) forces⁸ include spanwise thrust components.

$C_L/C_{L,0}$ is the lift with blowing on divided by the lift with blowing off. The data for the 60° delta were obtained from the investigation by Bradley and Wray.¹⁸ The results show that substantially more lift is generated by spanwise blowing on wings with lower sweep angles. The reason, of course, is related to the amount of vortex flow on the wing before blowing is applied. At $\alpha=21^\circ$, the 60° delta wing has a sizable amount of natural vortex lift as noted by the estimates of $C_{L,tot}/C_{L,0}$ in this figure, and by the lift trends discussed in Fig. 1.

Specific Excess Power

Although the spanwise blowing concept has demonstrated large beneficial aerodynamic effects, the true feasibility test is the integration of the spanwise thrust into the complete fighter aircraft design. Considerable work is necessary to obtain the desired spanwise blowing rates without severely penalizing the aircraft's main-engine thrust system, and to assure that the fighter with spanwise blowing is more maneuverable than the fighter without spanwise blowing. An attempt to demonstrate the possible effects of spanwise blowing on aircraft performance is made in Fig. 13, where the specific excess power available for maneuvering is presented as a function of load factor for the 45° delta-wing configuration. For demonstration purposes, an engine thrust and weight are assumed for the "aircraft," where the standard engine thrust is reduced by $C_\mu q_\infty S$ when spanwise blowing is utilized. The lift and drag forces used here are the total loads measured on the delta-wing configuration,⁸ and therefore, include the spanwise-blowing thrust components in the lift and drag directions.

The results show that spanwise blowing increases the specific excess power at load factors above 1, and allows higher load factors to be attained before reaching the lift

limit. These trends suggest that the improvements in the aerodynamic characteristics at high lifts are larger than the reductions in thrust associated with spanwise blowing. Although this illustrates a potential application to maneuvering aircraft, the practical aspects of propulsion integration and engine technology must be examined before the spanwise blowing concept can be exploited.

Concluding Remarks

An investigation has been conducted to determine the aerodynamic effects associated with blowing spanwise on wings of interest for fighter aircraft. This study summarizes the results of two wind-tunnel test programs,^{7,8} which were performed to obtain surface-pressure distributions on a 44° swept trapezoidal wing, and lift, drag, and pitching-moment data on delta, arrow, and diamond wing planforms having leading-edge sweeps of 30° and 45°.

The results of the pressure tests indicate that spanwise blowing has significant effects on the upper-surface pressure field at high angles of attack where the largest suction pressures occur at the inboard span station near the wing leading edge, and diminish outboard. The sectional effects of spanwise blowing are strongly dependent on angle of attack, jet thrust coefficient, and span location, the largest effects occurring at the highest angles of attack, thrust coefficients, and on the inboard portion of the wing. Full vortex section lift, as estimated by the leading-edge suction analogy, is achieved at the inboard span station with a small blowing rate, but successively higher blowing rates are necessary to attain the full vortex-lift level at increased span distances.

The results of the force tests on the family of wing planforms show that spanwise blowing generates large increments in lift at high angles of attack; improves the drag polars; and extends the linear pitching moment to high lifts. The leading-edge suction analogy provides good predictions for the aerodynamic characteristics that were obtained for the wings with a fully developed leading-edge vortex. Decreasing the wing's leading-edge sweep angle increases the amount of lift generated by blowing spanwise. In addition, integration of spanwise blowing concept into a fighter aircraft design offers the possibility of increasing specific excess power available for maneuvering at higher load factors.

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